# Characterization of different work hardening behavior in AISI 321 stainless steel and Hadfield steel

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**Abstract** In order to distinguish the difference between AISI 321 stainless steel and Hadfield steel in work hardening behavior, both the Hollomon analysis and the differential Crussard-Jaoul analysis were used to determine the strain hardening exponent as a function of the strain. The results showed that the differential Crussard-Jaoul analysis characterized the discrepancy between AISI 321 steel and Hadfield steel in work hardening behavior more accurately than the Hollomon analysis. The work hardening of AISI 321 stainless steel resulted mainly from interactions of dislocations. When the true strain was rather low, the work hardening of Hadfield steel also resulted mainly from interactions of dislocations. At high strains, twinning would occur in Hadfield steel. It was the occurrence of twins that led to unusual work hardening at larger strains in Hadfield steel.

## Introduction

Austenitic steels with low stacking fault energy (SFE), typical example of which include the AISI 321 stainless steel and Hadfield steel, are able to work hardening rapidly at room temperature. It is well known that the work hardening behaviors of austenitic steels are related mainly to stacking fault energy and the lower SFE, the greater work hardening [1]. The SFE of Hadfield steel is 50 mJ/m<sup>2</sup> [1] and that of AISI 321 stainless steel is less than 20 mJ/m<sup>2</sup> [2]. Therefore, it seems to be convincible that AISI 321 stainless steel should have better work hardening

ability than Hadfield steel. However, under heavy impact stress Hadfield steel exhibits unique work hardening and higher gouging wear resistance, which is not found in AISI 321 stainless steel. To date, little work has been done to explain this discrepancy.

Strain hardening exponent n is a key parameter for characterizing the work hardening behaviors of metals and alloys. The greater the value of *n* is, the greater the work hardening. The value of n is determined the most commonly by the Hollomon analysis based on Hollomon's equation,  $\sigma = K\varepsilon^n$ , where  $\sigma$  is the true stress,  $\varepsilon$  the total true strain and K a constant [3]. In other words, the value of n is determined from the slope of  $\ln \sigma$  versus  $\ln \varepsilon$  curve. For the most of metallic alloys, the value of n determined by the Hollomon analysis is considered a constant. However, although the difference in work hardening behavior between AISI 321 and Hadfield steel exists, the *n* value of AISI 321 steel determined by Hollomon analysis is around 0.48, being almost equal to that of Hadfield steel [2]. Obviously, the Hollomon analysis cannot distinguish the difference between AISI 321 stainless steel and Hadfield steel in work hardening behavior. Moreover, studies already showed that a single n value cannot represent an entire  $\ln \sigma - \ln \varepsilon$  relation [4]. Therefore, it is necessary to attain the instantaneous slope of the ln  $\sigma$ -ln  $\varepsilon$  curve to reflect the change of *n* value with the strain.

Differential Crussard–Jaoul (C–J) analysis was also used to determine the strain hardening exponent *n* based on Ludwik relation,  $\sigma = \sigma_0 + K\varepsilon^n$ , where  $\sigma_0$  and *K* are a constant [3]. In addition, some researches showed that the change of *n* value determined by the differential Crussard– Jaoul analysis could relate the work hardening behaviors of metals to the change in microstructures and plastic deformation mechanisms better than that determined by the Hollomon analysis [5–7]. Therefore, it is possible to

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explain the above discrepancy between AISI 321 stainless steel and Hadfield steel in work hardening behavior using the differential Crussard–Jaoul analysis.

In this paper, it was our aim to distinguish the difference between AISI 321 stainless steel and Hadfield steel in work hardening behavior using the differential Crussard–Jaoul analysis, especially at large deformation.

#### Methods of analysis

#### The Hollomon analysis

The Hollomon analysis assumes that the true stress  $\sigma$  versus total true strain  $\varepsilon$  curve is described by the power relationship [3]:

$$\sigma = K \varepsilon^{n^{\rm H}} \tag{1}$$

For the concise distinction between the strain hardening exponent determined by the Hollomon analysis and the differential Crussard–Jaoul analysis respectively, a superscript was used. The logarithmic form of Eq. 1 is:

$$\ln \sigma = \ln K + n^{\rm H} \ln \varepsilon \tag{2}$$

The value of  $n^{H}$  as a function of  $\varepsilon$  is obtained from the instantaneous slope of the curve. That is to say:

$$n^{\rm H} = \frac{\mathrm{d}\ln\sigma}{\mathrm{d}\ln\varepsilon} = \frac{\frac{1}{\sigma}\mathrm{d}\sigma}{\frac{1}{\varepsilon}\mathrm{d}\varepsilon} = \frac{\varepsilon\mathrm{d}\sigma}{\sigma\mathrm{d}\varepsilon} \tag{3}$$

The differential Crussard-Jaoul (C-J) analysis

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The differential Crussard–Jaoul (C–J) analysis is based on Ludwik relation [3]:

$$\sigma = \sigma_0 + K \varepsilon^{n^{c-j}} \tag{4}$$

The logarithmic form of Eq. 4, after differentiating with respect to  $\varepsilon$ , formally establishes the analysis method:

$$\ln \frac{d\sigma}{d\varepsilon} = \ln(n^{C-J}K) + (n^{C-J} - 1)\ln\varepsilon$$
(5)

The value of  $(n^{C-J} - 1)$  as a function of  $\varepsilon$  is obtained from the instantaneous slope of the  $\ln \frac{d\sigma}{d\varepsilon} - \ln \varepsilon$  curve. That is to say:

$$n^{\mathrm{C}-\mathrm{J}} - 1 = \frac{\mathrm{d}\ln\frac{\mathrm{d}\sigma}{\mathrm{d}\varepsilon}}{\mathrm{d}\ln\varepsilon} = \frac{\frac{\mathrm{d}\varepsilon}{\mathrm{d}\sigma}\frac{\mathrm{d}^{2}\varepsilon}{\mathrm{d}\varepsilon^{2}}\mathrm{d}\varepsilon}{\frac{1}{\varepsilon}\mathrm{d}\varepsilon} = \varepsilon\frac{\mathrm{d}\varepsilon}{\mathrm{d}\sigma}\frac{\mathrm{d}^{2}\sigma}{\mathrm{d}\varepsilon^{2}} \tag{6}$$

Thus,

$$n^{\rm C-J} = \varepsilon \frac{\mathrm{d}\varepsilon}{\mathrm{d}\sigma} \frac{\mathrm{d}^2 \sigma}{\mathrm{d}^2 \varepsilon} + 1 \tag{7}$$

### **Experimental procedures**

Experimental steels were melted and cast in vacuum induction furnace under argon atmosphere. Chemical

Table 1 Chemical compositions of two experimental alloys (wt%)

Alloys	С	Mn	Cr	Ni	Ti	Fe
Hadfield steel	1.10	13.30	_	_	_	Bal.
AISI 321 steel	0.07	-	17.80	7.92	0.52	Bal.

compositions of steels are listed in Table 1. The ingot were hot forged to bars 15 mm in diameter, and then bars were austenitized at 1373 K for 40 min, followed by a water quenching. Tested specimens were cylindrical and button headed, with a 50 mm gauge length and a 10 mm gauge diameter. The tensile tests were performed at a strain rate of  $6.67 \times 10^{-4}$  s<sup>-1</sup>.

## Results

Figure 1 shows the true stress  $\sigma$  versus total true strain  $\varepsilon$  curve of AISI 321 stainless steel and that of Hadfield steel, in which the elastic section and the close rupture section were cut off. Figure 2 shows the ln  $\sigma$ -ln  $\varepsilon$  curve determined from Fig. 1. Obviously, none of the curves shows a linear relation. Therefore, a single *n* value cannot represent an entire curve. To reflect the change of *n* value with the strain, it is necessary to attain the instantaneous slope of the ln  $\sigma$ -ln  $\varepsilon$  curve consist of lots of discrete points, we can calculate the difference quotient  $\Delta \sigma$  and  $\Delta \varepsilon$  instead of the differentiation  $d\sigma$  and  $d\varepsilon$  respectively. However, this method will introduce errors. To decrease the errors, we first simulated the  $\sigma$ - $\varepsilon$  curve and then calculated the differentiation.

Based on the fitted curves of a polynomial with the third degree (red dash line in Fig. 1), the strain hardening exponent  $n_{exp}^{H}$  of the experimental AISI 321 stainless steel



Fig. 1 Experimental and polynomial fitting true stress  $\sigma$  versus total true strain  $\varepsilon$  curves of AISI 321 stainless steel and Hadfield steel (the elastic section and the close rupture section were cut off; *black solid line* is experimental data, *red dash line* is polynomial fitting data)



Fig. 2 The  $\ln \sigma - \ln \epsilon$  curves of AISI 321 stainless steel and Hadfield steel determined from Fig. 1



Fig. 3 Strain hardening exponent  $n_{exp}^{H}$  determined by Hollomon analysis versus true strain  $\varepsilon$  curves of AISI 321 stainless steel and Hadfield steel

and Hadfield steel determined by Hollomon analysis are shown in Fig. 3, respectively. Both the  $n_{exp}^{H}$  of AISI 321 stainless steel and that of Hadfield steel increased with the strain. Note that when the strain was below about 0.16, the  $n_{exp}^{H}$  of AISI 321 stainless steel were almost equal to that of Hadfield steel. When the strain was over 0.16, however, the  $n_{exp}^{H}$  of Hadfield steel were greater than that of AISI 321 stainless steel, and the difference between them increased with further increasing the strain.

Figure 4 shows the strain hardening exponent  $n_{exp}^{C-J}$  of the experimental AISI 321 stainless steel and Hadfield steel determined by the differential Crussard–Jaoul analysis, respectively. In contrast with the  $n_{exp}^{H}$ , the  $n_{exp}^{C-J}$  of AISI 321 stainless steel decreased very slowly from 1 with increasing the strain. When the strain was lower than around 0.07, the  $n_{exp}^{C-J}$  of Hadfield steel remained constant and was almost equal to that of AISI 321 stainless steel. When the strain was over 0.07, however, it sharply increased with the strain.



**Fig. 4** Strain hardening exponents  $n_{exp}^{C-J}$  determined by differential Crussard–Jaoul analysis versus true strain  $\varepsilon$  curves of AISI 321 stainless steel and Hadfield steel

### Discussion

Work hardening is mainly attributed to interactions of dislocations and barriers which impede their motion through the crystal lattice. In addition, it is also confirmed that deformation twinning can result in the high work hardening rate in Hadfield steel [8, 9].

If the deformation is realized only by the dislocation slip,  $\varepsilon$  is equal to the strain  $\varepsilon_{dis}$  resulting from dislocation slip. Thompson [10] proposed that the strain increment  $d\varepsilon_{dis}$  can be given by the formula as following:

$$d\varepsilon_{\rm dis} = b\lambda d\rho_{\rm dis} \tag{8}$$

where  $\rho_{\rm dis}$  is the dislocation density, *b* the length of the Burgers vector and  $\lambda$  the slip length. Holt and Staker [11] proposed that  $\rho_{\rm dis}^{1/2}$  was proportional to the reciprocal of the slip length  $\lambda$ . Thus, Eq. 8 can be rewritten by substituting  $\rho_{\rm dis}^{-1/2} = \beta \lambda$ , where  $\beta$  is a constant.

$$d\varepsilon_{\rm dis} = b\beta^{-1}\rho_{\rm dis}^{-1/2}d\rho_{\rm dis} \tag{9}$$

 $\varepsilon_{\rm dis}$  can be obtained through integration of Eq. 9:

$$\varepsilon_{\rm dis} = 2b\beta^{-1}\rho_{\rm dis}^{1/2} \tag{10}$$

Mecking and Kocks [12] proposed the formula relating the stress to the change of dislocation density:

$$\sigma_{\rm dis} = \alpha G b \rho_{\rm dis}^{1/2} \tag{11}$$

where G is the shear modulus, b the length of the Burgers vector and  $\alpha$  a constant.

Substituting Eq. 10 into Eq. 11 gives:

$$\sigma_{\rm dis} = \frac{1}{2} \alpha G \beta \varepsilon_{\rm dis} \tag{12}$$

Differentiating Eq. 12 with respect to  $\varepsilon_{dis}$  yields the strain hardening rates due to interactions of dislocations:

$$\frac{\mathrm{d}\sigma_{\mathrm{dis}}}{\mathrm{d}\varepsilon_{\mathrm{dis}}} = \frac{1}{2} \alpha G \beta \tag{13}$$

Thus,

$$\frac{\mathrm{d}^2 \sigma_{\mathrm{dis}}}{\mathrm{d}\varepsilon_{\mathrm{dis}}^2} = 0 \tag{14}$$

Substituting Eqs. 12 and 13 into Eq. 3 gives:

$$n_{\rm dis}^{\rm H} = \frac{\varepsilon_{\rm dis} d\sigma_{\rm dis}}{\sigma_{\rm dis} d\varepsilon_{\rm dis}} = \frac{2}{\alpha G\beta} \cdot \frac{1}{2} \alpha G\beta = 1$$

Likewise, substituting Eq. 14 into Eq. 7 gives:

$$n_{\mathrm{dis}}^{\mathrm{C}-\mathrm{J}} = \varepsilon_{\mathrm{dis}} \frac{\mathrm{d}\varepsilon_{\mathrm{dis}}}{\mathrm{d}\sigma_{\mathrm{dis}}} \frac{\mathrm{d}^2\sigma_{\mathrm{dis}}}{\mathrm{d}\varepsilon_{\mathrm{dis}}^2} + 1 = 0 + 1 = 1$$

Therefore, the calculated strain hardening exponents resulting only from interactions of dislocations,  $n_{\rm dis}^{\rm H}$  and  $n_{\rm dis}^{\rm C-J}$ , are both a constant of 1. For experimental AISI 321 stainless steel and Hadfield steel, obviously, the calculated  $n_{\rm dis}^{\rm H}$  greatly deviates from their experimental results  $n_{\rm exp}^{\rm H}$ . However, the calculated  $n_{\rm dis}^{\rm C-J}$  of AISI 321 stainless steel accords well with its experimental result  $n_{\rm exp}^{\rm C-J}$ . For Hadfield steel, the calculated  $n_{\rm dis}^{\rm C-J}$  also accords well with the  $n_{\rm exp}^{\rm C-J}$  when the strain is lower than around 0.07.

If the deformation is realized only by the twining,  $\varepsilon$  is equal to the strain  $\varepsilon_{twin}$  resulting from the twining. The strain  $\varepsilon_{twin}$  can be calculated by the following formula [13]:

$$\varepsilon_{\rm twin} = \ln(1 + \Phi f) \tag{15}$$

where *f* is the volume fraction of twins and  $\Phi$  is the equivalent strain provided by twinning and can be evaluated by the formula:  $\Phi = S/M$ , where *S* is the twinning shear and *M* a Taylor factor [13]. Substituting S = 0.707 and M = 3.06 [14], gives  $\Phi = 0.231$ .

Differentiating both sides of Eq. 15 with respect to f and substituting  $\Phi = 0.231$  gives:

$$\mathrm{d}\varepsilon_{\mathrm{twin}} = \frac{0.231}{1 + 0.231f} \mathrm{d}f \tag{16}$$

Remy [15] proposed an expression relating the flow stress  $\sigma_{\text{twin}}$  to twinning:

$$\sigma_{\text{twin}} = K_{\text{T}}(2t)^{-1} \left(\frac{f}{1-f}\right)$$
(17)

where  $K_{\rm T}$  is a constant and t is the average thickness of twins. Thus, the stress increment  $d\sigma_{\rm twin}$  is obtained by the differentiation of Eq. 17 with respect to f:

$$d\sigma_{twin} = K_{T}(2t)^{-1} \frac{1}{(1-f)^{2}} df$$
(18)

Combining Eq. 16 into 18 gives:

$$\frac{\mathrm{d}\sigma_{\mathrm{twin}}}{\mathrm{d}\varepsilon_{\mathrm{twin}}} = K_{\mathrm{T}}(2t)^{-1} \frac{1+0.231f}{0.231(1-f)^2} \tag{19}$$

Thus,

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$$\frac{d^2\sigma_{\text{twin}}}{d\varepsilon_{\text{twin}}^2} = K_{\text{T}}(2t)^{-1} \frac{(9.658+f)(1+0.231f)}{0.231(1-f)^3}$$
(20)

Substituting Eqs. 15, 17 and 19 into Eq. 3 gives  $n_{\text{twin}}^{\text{H}}$ :

$$H_{\text{twin}}^{\text{H}} = \frac{(1+0.231f)\ln(1+0.231f)}{0.231f(1-f)}$$
(21)

Likewise, substituting Eqs. 15, 19 and 20 into Eq. 7 gives  $n_{\text{twin}}^{\text{C}-\text{J}}$ :

$$n_{\text{twin}}^{\text{C}-\text{J}} = \frac{(9.658 + f)\ln(1 + 0.231f)}{(1 - f)} + 1$$
(22)

Adler [8] quantified the twined volume fraction f in a Hadfield steel as a function of the total true strain  $\varepsilon$ , which are summarized in the Table 2. According to f, both the value of  $n_{\text{twin}}^{\text{C}-\text{J}}$  and that of  $n_{\text{twin}}^{\text{H}}$  of Hadfield steel were calculated, which is also listed in Table 2.

Figure 5 shows the comparisons between the experimental  $n_{exp}^{C-J}$ , calculated  $n_{dis}^{C-J}$  and  $n_{twin}^{C-J}$  resulting only from dislocation slip and the twinning, respectively. When the strain is lower than 0.05, both the  $n_{exp}^{C-J}$  of Hadfield steel and that of AISI 321 stainless steel is almost equal to 1, which coincides with the calculated  $n_{dis}^{C-J}$ ; when the strain is over 0.05, the  $n_{exp}^{C-J}$  of Hadfield steel rapidly increases with the strain, which is coincident with the tendency of the  $n_{twin}^{C-J}$ . Note that the  $n_{twin}^{C-J}$  of Hadfield steel is greater than the  $n_{exp}^{C-J}$ at the same strain. For AISI 321 stainless steel, twinning hardly occurs at room temperature [16], thus its work hardening is mainly attributed to interactions of dislocations with each other.

Remy [15] proposed a twin nucleation model for predicting the critical resolved shear stress:

$$\frac{1}{\sqrt{3}} \left[ \frac{1}{3} + K \frac{\tau_{\rm T}}{G} \right] \cdot \frac{\tau_{\rm T}}{G} = \frac{\gamma}{Gb}$$
(23)

**Table 2** The comparison between the experimental strain hardening exponent  $n_{\text{exp}}^{\text{H}}$  and  $n_{\text{exp}}^{\text{C-J}}$  and the calculated  $n_{\text{twin}}^{\text{H}}$  and  $n_{\text{twin}}^{\text{C-J}}$  in Hadfield steel

ĉ <sub>Р</sub>	$f^{\mathrm{a}}$	$n_{\rm exp}^{\rm H}$	$n_{\rm twin}^{\rm H}$	$n_{\mathrm{exp}}^{\mathrm{C-J}}$	$n_{\rm twin}^{\rm C-J}$	
0.04	0	0.25	1.0	0.98	1.0	
0.06	0.05	0.34	1.06	0.98	1.12	
0.18	0.18	0.65	1.24	1.28	1.49	
0.30	0.25	0.93	1.37	1.76	1.74	

<sup>4</sup> The twined volume fraction f was derived from Adler [8]



**Fig. 5** Comparison between the experimental strain hardening exponents  $n_{\exp}^{C-J}$ , calculated  $n_{dis}^{C-J}$  due to dislocations interaction in AISI stainless steel and  $n_{twin}^{C-J}$  due to twinning in Hadfield steel

where  $\tau_{\rm T}$  is the critical resolved shear stress,  $\gamma$  stacking fault energy, *K* a constant, *G* the shear modulus and *b* the Burgers vector. Substituting  $\gamma = 50 \text{ mJ/m}^2$  [2], G = 70 GPa [17] and K = 700 [15] into Eq. 23 gives:

 $\tau_T=168.5 \text{ MPa}$ 

According to Taylor's theory [14], i.e.  $\sigma_{\rm C} = 3.06\tau_{\rm T}$ , the critical stress  $\sigma_{\rm C}$  of 515.6 MPa is determined. The corresponding critical strain is around 0.037 determined from Fig. 1. In other words, the twinning cannot take place when the strain is below 0.037 in the present Hadfield steel. Accordingly, the work hardening of Hadfield steel results only from interactions of dislocations with each other when the strain is below 0.037. This result is well agreement with our result that the  $n_{exp}^{C-J}$  of Hadfield steel is almost equal to the  $n_{\rm dis}^{\rm C-J}$  when the strain is lower than 0.05 (Fig. 5). Twinning will occur when the strain is over 0.037. Therefore, the outstanding work hardening property of high manganese steel at high strain results mainly from the occurrence of twinning. On the other hand, the slip and the twinning are regarded as competing mechanisms. If twinning occurs, it will reorient the crystals lattice, favoring the further basal slip. Thus, deformation will be realized by both slip and twinning. In such a case, the slip length is significantly reduced due to the formation of twins [18], thus cross-slip will readily take place with dislocations pile-up, leading to the occurrence of dynamic recovery and work softening [19]. This may be the reason why the  $n_{exp}^{C-J}$  of Hadfield steel is lower than the  $n_{twin}^{C-J}$ .

#### Conclusions

The differential Crussard–Jaoul analysis more accurately described and characterized the discrepancy between AISI 321 stainless steel and Hadfield steel in work hardening behavior than the Hollomon analysis. The work hardening of AISI 321 stainless steel mainly resulted from interactions of dislocations. At low strains, the work hardening of Hadfield steel also resulted from interactions of dislocations. When the strain is larger, twinning will occur. It was the occurrence of twinning that led to unusual work hardening at larger strains in Hadfield steel.

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### References

- 1. Danaf EE, Kalidindi SR, Doherty RD (1999) Metall Mater Trans A 30:1223
- 2. Dastur YN, Leslie WC (1981) Metall Trans A 12:749
- Sinha AK (2003) Physical metallurgy handbook. McGraw Hill, Boston
- 4. Bowen AW, Partridge PG (1974) J Phys D Appl Phys 7:969
- 5. Soussan A, Degallaix S, Magnin T (1991) Mater Sci Eng A 142:169
- Umemoto M, Liu ZG, Sugimoto S, Tsuchiya K (1999) Metall Mater Trans A 31:1785
- Mejia I, Maldonado C, Benito JA, Jorba J, Roca A (2006) Mater Sci Forum 509:37
- 8. Adler PH, Olson GB, Owen WS (1986) Metall Trans A 17:1725
- Bayraktar E, Khalid FA, Levaillant C (2004) J Mater Process Technol 147:145
- Thompson AW, Baskes MI, Flanagan WF (1973) Acta Metall 21:1017
- 11. Staker MR, Holt DL (1972) Acta Metall 20:569
- 12. Mecking H, Kocks UF (1981) Acta Metall 29:1865
- Keshavan MK, Sargent G, Conrad H (1975) Metall Trans A 6:1291
- 14. Remy L (1981) Metall Trans A 12:387
- 15. Remy L (1978) Acta Metall 26:443
- Karaman I, Sehitoglu H, Chumlyakov YI, Maier HJ (2002) J Miner Met Mater Soc 7:31
- 17. Hutchinson B, Ridley N (2006) Scr Mater 55:299
- 18. Kalidindi SR (1998) Int J Plast 14:1265
- 19. Jackson PJ (1985) Prog Mater Sci 29:139